

## Structure and elastic properties of quartz at pressure

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### Abstract

Unit cells and crystal structures were determined on a single crystal of quartz at seven pressures from 1 atm to 61.4 kbar. Unit-cell parameters are  $a = 4.916(1)$  and  $c = 5.4054(4)\text{\AA}$  at 1 atm, and  $a = 4.7022(3)$  and  $c = 5.2561(2)\text{\AA}$  at 61.4 kbar. Structural changes observed over this pressure range include a decrease in the Si-O-Si angle from  $143.73(7)^\circ$  to  $134.2(1)^\circ$ , a decrease in the average Si-O bond distance from  $1.6092(7)$  to  $1.605(1)\text{\AA}$ , and an increase in distortion of the silicate tetrahedron. Several O-O distances show very large changes (11%) that can be related to the unit-cell-edge compression. As pressure is increased, the geometry of the SiO<sub>2</sub> (quartz) structure approaches that of the low-pressure GeO<sub>2</sub> (quartz) structure.

The structural changes that take place with increased temperature are not the inverses of those that occur with increased pressure; changes in the Si-O-Si angle and the tetrahedral tilt angle control thermal expansion, whereas smaller changes in the Si-O-Si angle and tetrahedral distortion control isothermal compression.

By constraining the zero-pressure bulk modulus to be equal to that calculated from acoustic data [ $K_T = 0.371(2)$  Mbar], the pressure derivative of the bulk modulus at zero pressure [ $K_T' = 6.2(1)$ ] has been calculated by fitting the  $P$ - $V$  data to a Birch-Murnaghan equation of state. The anomalously low value of Poisson's ratio in quartz can be explained by the low ratio of the off-diagonal shear moduli to the pure-shear moduli. This small ratio reflects the easily expanding or contracting spirals of tetrahedra that behave like coiled springs.

### Introduction

The literature on the crystal structure and compressibility of quartz leaves many questions about its changes with pressure. As high-pressure structural refinements have not been as precise as those performed under ambient conditions, these studies report large changes (e.g., the Si-O-Si interbond angle); however, subtle ones have not been previously resolvable. Recent experimental developments in our laboratory offer the potential of providing improved resolution in high-pressure structural data.

The crystal structure of quartz at room temperature and pressure has been refined many times (Young and Post, 1962; Smith and Alexander, 1963; Zachariassen and Plettinger, 1965; Le Page and Donnay, 1976; Jorgensen, 1978; d'Amour *et al.*, 1979),

with the Young and Post and the Smith and Alexander papers reporting the first quality refinements of positional parameters and thermal ellipsoids. Zachariassen and Plettinger improved upon these studies by applying a secondary-extinction correction to their refinement. The Le Page and Donnay refinement again improved the R value; however, no corrections for crystal X-ray absorption or extinction were made. Both Jorgensen and d'Amour *et al.* collected intensity data for room-pressure structural refinements with crystals already loaded in high-pressure cells; these refinements are of lower precision than the others.

Static-compressibility studies on quartz were first carried out by Adams and Williamson (1923) and Bridgman (1925; 1928), and then greatly improved by Bridgman (1948a,b; 1949) and others (McWhan, 1967; Vaidya *et al.*, 1973; Olinger and Halleck, 1976; Jorgensen, 1978; d'Amour *et al.*, 1979). McWhan measured the compression of quartz in a modified Bridgman-anvil apparatus with Guinier geometry

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Table A-1: Observed and calculated structure factors for quartz at 37.6 kbar.

L OBS		CALC		L OBS		CALC		L OBS		CALC		L OBS		CALC		L OBS		CALC																	
-4	-4	L	L	-3	-3	L	L	-2	-2	L	L	0	0	-2	-2	L	L	1	1	2	2	L	L	2	2	3	3	L	L	3	3	4	4	L	L
-3	25	21	21	-4	59	56	56	-8	49	52	52	-6	158	158	158	-6	45	47	47	-6	16 <sup>a</sup>	11	11	-4	76	76	76	-4	41	38	38	-4	41	38	38
-2	1	68	68	-3	97	94	94	-7	124	20	20	-5	26	22	22	-5	125	24	24	-3	43	43	43	-3	127	128	128	-3	127	128	128				
-1	18 <sup>a</sup>	20	20	-1	47	47	47	-6	85	89	89	0	-1	L	L	-4	67	70	70	-2	69	70	70	-2	61	63	63	-2	61	63	63				
0	19 <sup>a</sup>	20	20	0	152	151	151	-5	94	92	92	-1	166	170	170	-3	11 <sup>a</sup>	10	10	-1	67	68	68	-1	59	60	60	-1	59	60	60				
1	21	20	20	2	8 <sup>c</sup>	14	14	-4	112	110	110	-8	77	76	76	-2	83	83	83	4	30	23	23	4	30	23	23	4	30	23	23				
-4	-3	L	L	-3	-2	L	L	-1	117	118	118	-6	11 <sup>a</sup>	11	11	-1	33	33	33	4	1	L	L	4	1	L	L	4	1	L	L				
-5	11 <sup>a</sup>	17	17	-7	23	12	12	-2	-1	L	L	0	144	145	145	1	3	L	L	2	4	L	L	2	4	L	L	2	4	L	L				
-4	76	74	74	-6	14 <sup>a</sup>	11	11	-8	55	54	54	0	0	L	L	-5	39	44	44	-4	41	38	38	-4	41	38	38								
-3	47	46	46	-5	126	124	124	-7	98	98	98	-6	82	80	80	-3	79	80	80	-3	43	43	43	-3	43	43	43								
-2	72	71	71	-4	68	70	70	-6	44	47	47	0	0	0	0	-3	101	101	101	-2	43	39	39	-2	43	39	39								
-1	68	68	68	-3	11 <sup>a</sup>	10	10	-5	25	22	22	9	127	125	125	4	41	42	42	-1	81	85	85	-1	81	85	85	-1	81	85	85				
5	64	58	58	-2	85	83	83	-3	175	173	173	0	127	125	125	6	37	58	58	0	81	85	85	0	50	52	52	0	50	52	52				
-4	-2	L	L	-1	33	-31	-31	-1	170	169	169	0	1	L	L	2	-1	L	L	3	0	L	L	1	110	114	114	1	110	114	114				
-5	50	49	49	2	20	7	7	-2	0	L	L	-9	38	38	38	-6	86	87	87	-5	26	31	31	2	78	75	75	2	78	75	75				
-4	68	67	67	-3	-1	L	L	-6	99	97	97	-7	11 <sup>a</sup>	8	8	-5	131	134	134	-4	84	85	85	-4	84	85	85	-4	84	85	85				
-3	37	43	43	-7	90	90	90	8	20	10	10	-1	195	192	192	-4	144	146	146	3	1	L	L	3	1	L	L	3	1	L	L				
-2	30	39	39	-6	59	62	62	-1	-3	L	L	0	2	L	L	-6	9 <sup>a</sup>	10	10	-7	44	43	43	-5	58	57	57	-5	58	57	57				
-1	84	85	85	-5	36	44	44	-6	57	57	57	-7	76	72	72	-8	9 <sup>a</sup>	10	10	-5	87	91	91	-4	64	62	62	-4	64	62	62				
4	64	62	62	-4	77	79	79	-5	91	90	90	-5	9 <sup>a</sup>	2	2	-7	48	48	48	-3	106	104	104	-3	106	104	104	-2	104	104	104				
5	55	57	57	-3	104	100	100	-4	38	42	42	-7	76	72	72	-5	93	93	93	7	92	90	90	-1	70	70	70	-1	70	70	70				
-4	-1	L	L	7	49	43	43	-3	105	104	104	-1	-1	L	L	-5	93	93	93	0	97	97	97	0	97	97	97	0	97	97	97				
-3	44	41	41	-3	0	L	L	-6	57	60	60	2	1	L	L	-7	50	46	46	3	2	L	L	3	2	L	L	3	2	L	L				
-2	75	75	75	-5	62	65	65	-1	-2	L	L	-8	57	60	60	-6	16 <sup>a</sup>	5	5	-7	50	46	46	-5	58	58	58								
-1	112	114	114	-4	25	24	24	-8	37	25	25	-7	31	26	26	-5	49	51	51	-4	153	152	152	-4	153	152	152								
0	51	52	52	-2	-4	L	L	-7	37	25	25	-6	102	103	103	-3	17 <sup>a</sup>	36	36	-3	17 <sup>a</sup>	36	36	-3	17 <sup>a</sup>	36	36								
1	60	60	60	-7	37	25	25	-6	102	103	103	-5	121	119	119	-2	12 <sup>a</sup>	7	7	-4	15 <sup>a</sup>	23	23	-4	15 <sup>a</sup>	23	23								
2	61	62	62	-3	39	41	41	-5	121	119	119	-1	309	309	309	-1	162	160	160	-3	44	43	43	-3	44	43	43								
3	127	128	128	-2	105	103	103	-3	39	41	41	-1	171	168	168	0	35	37	37	-2	45	48	48	-2	45	48	48								
4	32	39	39	-1	70	70	70	-1	171	168	168	1	1	L	L	7	14 <sup>a</sup>	12	12	-1	85	84	84	-1	85	84	84								
-3	-4	L	L	0	99	98	98	0	36	36	36	-9	36	39	39	2	2	L	L	0	26	20	20	0	26	20	20								
-4	25	22	22	-2	-3	L	L	-1	-1	L	L	-8	34	37	37	3	3	L	L	5	5 <sup>a</sup>	17	17	5	5 <sup>a</sup>	17	17								
-3	45	42	42	-7	52	46	46	-8	34	37	37	-7	92	90	90	-7	12 <sup>a</sup>	9	9	4	4	L	L	4	4	L	L								
-2	47	48	48	-6	7 <sup>a</sup>	5	5	-7	92	90	90	-6	87	86	86	-6	51	50	50	-3	22	21	21	-3	22	21	21								
-1	83	84	84	-5	49	51	51	-6	87	86	86	-5	136	134	134	-5	38	38	38	-2	65	68	68	-2	65	68	68								
0	19 <sup>a</sup>	20	20	-4	151	152	152	-5	136	134	134	-4	142	146	146	-4	61	56	56	-1	24	20	20	-1	24	20	20								
-3	-3	L	L	-3	29	36	36	-3	129	125	125	-1	116	118	118	-3	98	94	94	0	0	0	0	0	0	0	0								
-7	12 <sup>a</sup>	8	8	-1	149	147	147	-1	1	L	L	7	22	20	20	-2	2 <sup>a</sup>	16	16	-1	46	47	47	-1	46	47	47								
-6	49	50	50	0	97	97	97	-7	82	83	83	1	2	L	L	0	148	151	151	0	148	151	151	0	148	151	151								
-5	36	38	38	-7	82	83	83	-8	54	54	54	-7	100	98	98	2	21	21	21	2	21	21	21	2	21	21	21								



Table A-1: Observed and calculated structure factors for quartz at 55.8 kbar.

L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC	L	OBS	CALC
-3	26	24	-2	26	25	-4	114	114	-7	79	80	-8	53	50	-3	10 <sup>a</sup>	12	-4	54	53
-2	71	66	0	160	157	-3	116	116	-6	15	15	-7	100	97	-2	81	80	-1	55	59
0	29	35	1	29	29	0	113	113	-3	137	137	-6	50	52	-1	39	41	4	1	L
-4	-3	L	-3	-2	L	-2	-1	L	0	-2	L	-3	172	175	2	4	L	-4	54	53
-5	18	23	-7	18	18	-8	49	50	-6	147	148	-1	167	171	-2	36	32	-3	121	120
-4	75	74	-5	110	114	-7	98	97	0	-1	L	1	3	L	3	0	L	-2	60	58
-2	82	81	-4	70	73	-3	174	175	-8	85	84	-5	43	44	-5	29	32	0	57	57
-1	37	39	-3	10 <sup>a</sup>	12	-1	167	171	-6	9 <sup>a</sup>	15	-4	69	67	-4	89	88	1	93	103
4	32	32	-2	79	80	5	118	117	0	140	141	-3	111	111	-4	89	88	2	79	79
5	55	55	-1	41	42	-2	0	L	0	140	141	-5	29	32	-4	89	88	3	46	41
-4	-2	L	7	46	46	-2	0	L	0	0	L	2	-1	L	5	62	62	4	2	L
-3	46	45	-3	-1	L	-6	100	98	-9	121	120	-6	97	97	-7	33	38	-5	55	54
-4	68	68	-6	64	64	-2	172	170	-6	69	66	-5	132	134	-6	60	59	-4	68	67
-3	29	35	-5	42	44	-1	-3	L	0	0	0	2	0	L	-5	95	96	-3	29	30
-2	31	33	-4	66	67	-6	59	59	0	1	L	-8	20	6	-4	34	37	-2	104	103
-1	97	98	-3	113	111	-5	96	96	-7	9 <sup>a</sup>	11	-7	49	50	-3	116	114	-1	69	70
4	63	67	7	40	38	-4	35	37	-3	12	8	-5	105	104	6	63	63	0	88	88
5	55	54	-3	0	L	-3	114	114	-1	180	179	-2	175	168	-3	2	L	3	32	35
-4	-1	L	-4	15	16	-1	-2	L	0	2	L	2	1	L	-7	47	46	5	42	45
-3	45	41	-2	76	79	-8	60	58	-7	83	85	-8	60	58	-6	6 <sup>a</sup>	10	-5	57	54
-2	76	79	-7	18	12	-7	18	12	-7	21	13	-7	21	13	-5	53	51	4	3	L
-1	104	103	-3	27	29	-6	100	101	-5	8 <sup>a</sup>	4	-6	102	101	-4	150	148	-5	57	54
0	55	57	-2	101	103	-3	39	39	-3	39	39	-6	102	101	-3	52	51	-4	47	42
1	62	64	-1	72	70	-1	166	164	1	-1	L	-5	117	117	-2	21	10	-3	47	32
2	56	58	0	89	88	0	38	39	-3	40	38	-3	40	38	-1	146	145	-2	34	31
3	121	120	4	49	53	5	24	23	-8	93	93	0	166	164	0	93	94	-1	84	84
-3	-4	L	-2	-3	L	-1	-1	L	-6	51	54	0	37	40	7	22	18	4	75	74
-3	42	42	-6	13 <sup>a</sup>	10	-9	37	39	1	0	L	2	2	L	3	3	L	5	25	23
-2	30	31	-5	50	51	-8	34	37	-9	11 <sup>a</sup>	15	-8	55	56	-6	48	46	4	4	L
-1	84	84	-4	147	148	-8	34	37	-9	304	304	-6	84	84	-4	51	50	-3	25	24
0	10 <sup>a</sup>	15	-3	51	51	-7	92	91	-1	304	304	-5	91	93	-3	97	96	-2	69	66
3	40	38	-2	7 <sup>a</sup>	10	-3	130	128	1	1	L	-4	115	114	-1	27	29	-1	20	19
-3	-3	L	0	93	94	-1	0	L	-9	39	40	-3	116	115	0	144	157	0	35	35
-7	16 <sup>a</sup>	11	-2	-2	L	-9	37	39	-8	31	37	0	114	112	2	27	26			
-6	47	46	-8	54	56	-7	9 <sup>a</sup>	8	-8	31	37	2	3	L	3	4	L			
-5	31	31	-7	30	31	-6	98	90	-7	93	90	-6	16	17	-3	40	37			
-4	52	50	-6	85	84	-5	133	134	-6	133	134	-5	114	114	-3	114	114			
-3	97	96	-5	92	92	-3	129	128	-3	129	128	-4	75	73	-2	82	81			



